A discrete type of universality theorem for L-functions attached to holomorphic normalized newforms is given. A similar discrete universality for the derivatives of those L-functions is also discussed, and an application to the distribution of zeros of derivatives of L-functions is presented. (A joint work with A. Laurincikas and J. Steuding.)