Since 1990, several families of parametrized Thue equations $F_{a}(X, Y)= \pm 1$ of positive discriminant have been solved, where $F_{a}$ is a binary irreducible form of degree at least 3 whose coefficients are polynomials in the parameter $a$. Typical results are that the family only has some trivial integer solutions $X, Y$ when $a$ is a sufficiently large integer. In the last few years, such families have also been studied when the parameter $a$ is an element of some quadratic algebraic number field. The talk will present these and related results.

